Semirings are generalizations of both unitary rings and bounded distributive lattices. We present a variety of semirings that is generated by a three-element subdirectly irreducible member, is locally finite and residually large and has a solvable word problem.